

Extreme Harmonic Generation in Electrically Driven Spin Resonance

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We report the observation of multiple harmonic generation in electric dipole spin resonance in an InAs nanowire double quantum dot. The harmonics display a remarkable detuning dependence: near the interdot charge transition as many as eight harmonics are observed, while at large detunings we only observe the fundamental spin resonance condition. The detuning dependence indicates that the observed harmonics may be due to Landau-Zener transition dynamics at anticrossings in the energy level spectrum.

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Electron spin resonance and nuclear magnetic resonance are powerful probes of condensed matter systems [1,2]. Electron spin resonance is widely used for quantum control of spin systems, including lithographically defined quantum dots [3] and nitrogen-vacancy centers in diamond [4]. Nuclear magnetic resonance has resulted in many discoveries in condensed matter physics, such as dynamic nuclear polarization [5], the Overhauser effect [6], and double resonance [7]. In a typical spin resonance experiment a static magnetic field B Zeeman splits the spin states, while an oscillating perpendicular magnetic field with frequency f drives coherent spin rotations, known as Rabi oscillations. Electron spin rotations occur when the resonance condition $hf = g\mu_B B$ is met. Here h is Planck's constant, g is the electronic g factor, and μ_B is the Bohr magneton. Driving the spin with a detuning large compared to the on-resonance Rabi frequency greatly suppresses the coherent rotations [8].

While electron spin resonance is usually performed on macroscopic ensembles, where the sample size is large enough to directly detect the magnetization, it is difficult to apply it directly to nanoscale systems, such as quantum dots [9]. This has led to the development of single spin resonance, where oscillating magnetic fields are generated via current carrying striplines [10], or effective ac magnetic fields are generated by electrically driving the electron in a strong spin-orbit material [11–14], a magnetic field gradient [15,16], or a spatially varying hyperfine field [17]. In quantum dot experiments spin readout is performed using spin-to-charge conversion, where the dc current through the double quantum dot (DQD) is measured in the presence of microwave driving or a local charge sensor is used to detect a spin-dependent tunneling event in the device [18].

In this Letter we present a detailed study of electric dipole spin resonance (EDSR) in an InAs nanowire DQD [19]. We observe strong harmonic generation in EDSR at driving frequencies satisfying the condition $nhf = g\mu_B B$, with n an integer as large as 8 in our system. Several earlier works showed harmonic generation with $n = 2$ [20–22],

but with little discussion of the result or mechanism. While some theories predict harmonic generation in electrically driven quantum dots [23–25], the origin of the harmonics remains unclear, as detailed quantitative measurements are absent.

A key finding of our measurements is that the presence of harmonics is strongly linked to the detuning of the DQD energy levels. For example, near the interdot charge transition we observe up to $n = 8$ harmonics in the EDSR response. In contrast, when far detuned from the interdot charge transition we only observe the fundamental EDSR response with $n = 1$. Our observations link the presence of harmonics to anticrossings in the DQD energy level diagram, suggesting the harmonics are caused by Landau-Zener transition dynamics [26,27]. We also observe an even or odd structure in the EDSR response near zero detuning, where odd harmonics result in increased Pauli blockade leakage current, while even harmonics show a suppression of current. Detailed measurements show a strong sinusoidal modulation of the resonant current with detuning. The data provide very clear signatures that can be used for comparison with future theoretical work.

We perform experiments in quantum dots defined along the length of an InAs nanowire [see Fig. 1(a)]. A single 50 nm diameter nanowire is placed on top of prepatterned Ti/Au depletion gates [28]. The nanowire and gates are separated by a 20 nm thick layer of SiN_x , which serves as a gate dielectric. We probe spin physics by defining a DQD using the four gates labeled lw , lp , rp , and rw . We then make use of Pauli blockade, where the interdot tunneling process is spin selective. Figure 1(b) plots the current I as a function of the gate voltages V_{lp} and V_{rp} , showing finite-bias triangles [29] for the $(5, 1) \leftrightarrow (6, 0)$ electron transition. Here we label states (N_l, N_r) , where N_l (N_r) is the number of electrons in the left (right) dot. As shown in the top panel of Fig. 1(c), with the DQD biased below the singlet-triplet splitting (E_{st}), singlet state tunneling is allowed, while current is blocked when the electrons are in a spin-triplet

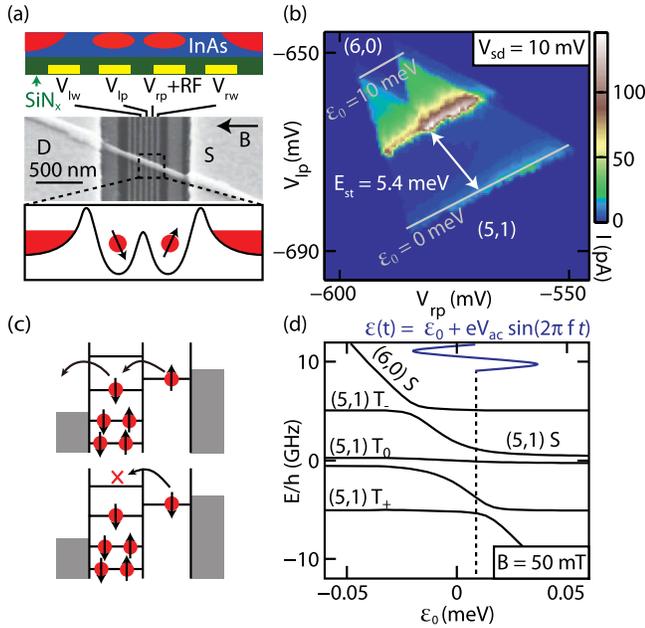


FIG. 1 (color online). (a) Scanning electron micrograph illustrating the sample geometry. Negative voltages applied to gates below the nanowire form a DQD. A magnetic field is applied in the plane of the substrate. (b) Current I as a function of gate voltages V_{lp} and V_{rp} showing finite bias triangles for the $(5, 1) \leftrightarrow (6, 0)$ charge transition. Transport is strongly suppressed for $\epsilon_0 < 5.4$ meV due to Pauli blockade. (c) Transport in the sequential tunneling regime. With $\epsilon_0 < E_{st}$, singlet state tunneling is allowed and triplet state tunneling is Pauli blocked. (d) Energy levels as a function of ϵ_0 .

configuration [lower panel of Fig. 1(c)] [3,18]. The resulting suppression of current due to Pauli blockade is clearly visible in Fig. 1(b). Measurements of a nonzero leakage current in the Pauli blockade regime are indicative of spin dynamics that rotate a Pauli-blocked triplet state to a singlet state. In Fig. 1(d) we plot the level diagram of the DQD as a function of detuning ϵ_0 [29]. Interdot tunneling t_c couples the singlet states $(5, 1)S$ and $(6, 0)S$, resulting in an anticrossing. For this device configuration we estimate $t_c < k_B T_e$, where $T_e = 150$ mK is the electron temperature. The curvature of the $(5, 1)T_0$ level is due to the g -factor difference between the dots. The $(6, 0)S$ state is coupled to the $(5, 1)T_+$ and T_- states by spin-orbit and hyperfine interactions [22,30].

We set ϵ_0 by changing the voltages V_{lp} and V_{rp} along the detuning axis shown in Fig. 2(a) (see the Supplemental Material [31]). EDSR transitions are then generated by applying a microwave drive tone at frequency f to gate rp . As a result, the detuning becomes time dependent with $\epsilon(t) = \epsilon_0 + eV_{ac} \sin(2\pi ft)$. This results in broadening of the finite-bias triangles shown in Fig. 2(a), which are measured with $2eV_{ac} = 1.8$ meV. EDSR experiments have generally been carried out deep in the Pauli-blocked region,

such as at the point labeled by the star in Fig. 2(a). Figure 2(c) shows the leakage current I measured at this point as a function of f and B . We observe a peak in I around $B = 0$, consistent with a hyperfine mediated spin mixing process with root-mean-square nuclear field $B_N \sim 3.5$ mT [32,33]. We also measure an enhancement in I when the electron spin resonance condition $hf = g_i \mu_B B$ is met, where g_i is the g factor on the i^{th} dot. Within the sensitivity limits of our current measurement (noise floor of 100 fA) we do not observe any clear evidence of harmonic generation at large detunings; i.e., there is no observable harmonic response for $n > 1$.

In stark contrast, Fig. 2(d) shows I as a function of B and f , this time measured at the interdot charge transition where $\epsilon_0 = 0$ [indicated by a circle in Fig. 2(a)]. Unlike the data in Fig. 2(c), we observe an EDSR response at many harmonics when $nhf = g_i \mu_B B$, indicating extreme harmonic generation in the DQD device. The EDSR harmonics are particularly strong since the signal weakens only slowly with increasing n , demonstrated by the fact that we readily resolve the $n = 8$ harmonic. The striking detuning dependence suggests that the presence of harmonics in the EDSR response is related to repeated passages through anticrossings in the energy level diagram near $\epsilon_0 = 0$.

Additionally, we observe an even or odd structure, wherein the odd harmonics result in an enhancement of the current, meaning spin blockade is lifted by the action of the microwaves. The even harmonics, on the other hand, feature a reduction in the current, indicating that spin blockade is enhanced. Finally, in Fig. 2(d) the signal coming from the even harmonics is stronger: while we clearly resolve even harmonics up to $n = 8$, the odd harmonics become very weak beyond $n = 3$.

We further study the harmonics by measuring their detuning dependence. Figure 3(a) shows I as a function of ϵ_0 and B for $f = 4.86$ GHz and $2eV_{ac} = 2.6$ meV. The resonant signal is clearly visible for the $n = 1$ through $n = 3$ harmonics and features clear oscillations as a function of ϵ_0 . The off-resonance leakage current is nonzero due to spin-orbit and hyperfine mediated relaxation processes and varies slowly with ϵ_0 [33]. To examine the resonant response in greater detail we subtract off the nonresonant “background” to obtain ΔI_{res} , the change of the leakage current due to resonant microwaves. We plot this quantity as a function of ϵ_0 for the dot with $g = 7.8$ in Fig. 3(b) (see the Supplemental Material [31]). Inside the region where $|\epsilon_0| < eV_{ac}$ the resonant current exhibits sinusoidal oscillations as a function of ϵ_0 . For several values of ϵ_0 , ΔI_{res} is less than zero, meaning the resonant microwaves interfere with other spin-relaxation processes. With increasing n , the frequency of the oscillations in ΔI_{res} increases, making additional peaks visible. For odd harmonics, the oscillations feature a local maximum at zero detuning, while for the even harmonics they feature a local minimum.

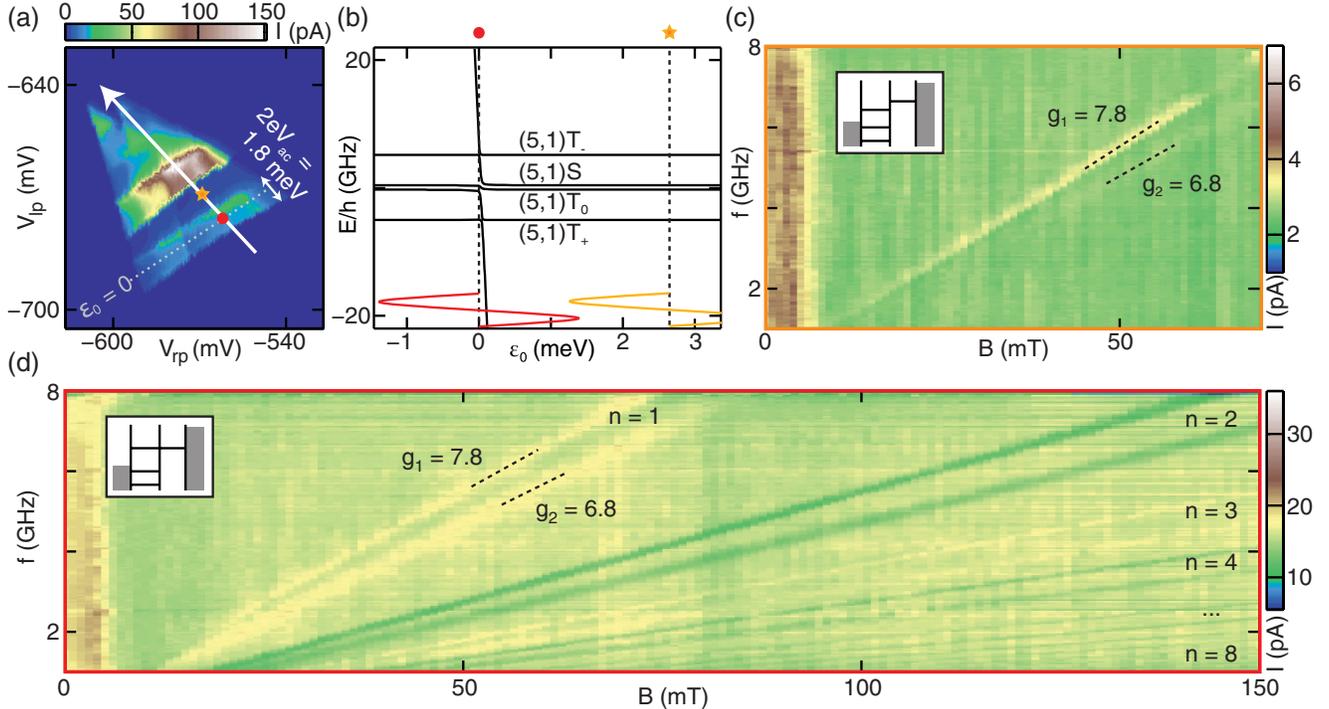


FIG. 2 (color online). (a) I as a function of V_{lp} and V_{rp} . Microwave driving with $f = 4$ GHz and $2eV_{ac} = 1.8$ meV broadens the features in the charge stability diagram. A white line indicates the detuning axis. (b) Energy level diagram with the ac excitation drawn to scale in the zero detuning region (circle) and the far detuned region (star). (c) I as a function of B and f , taken at $\epsilon_0 = 2.6$ meV, labeled by a star in (a). (d) I as a function of B and f , taken near $\epsilon_0 = 0$, indicated by the circle in (a). We observe up to $n = 8$ harmonics in the EDSR response. The approximate level configurations are shown in the insets.

This behavior is particularly visible as the even or odd structure in Fig. 2(d).

In Figs. 3(c)–3(d) we explore the effect of the amplitude of the applied microwaves on the resonant response by plotting the $n = 2$ and $n = 1$ resonant signals for $2eV_{ac} = 1, 1.8, 2.6,$ and 3.4 meV. With increasing driving the amplitude of the oscillations in ΔI_{res} decreases. For $n = 1$ the peak current at zero detuning drops from 2.5 to 0.5 pA. The frequency of the oscillations also appears to decrease, such that the number of visible peaks for each harmonic remains roughly constant. Data for $n = 3$ and $n = 4$, not shown here, exhibit the same trends.

The measurements presented in Fig. 3 provide very clear signatures that can be used for comparison with future theoretical work. A concrete comparison will require a theory that takes into account the noise sources that are inherent to semiconductor DQDs. Of particular interest is detuning noise, which is significant in these devices (typically on the order of $20 \mu\text{eV}$ [34,35]). Additionally, fluctuating nuclear fields and dynamic nuclear polarization processes may be key elements that lead to the interesting even or odd dependence observed in Fig. 2(d) [36,37].

To examine the role of the electron occupancy on the harmonics, we repeated the experiments at two other

Pauli-blocked interdot transitions. Data from the $(5,1) \leftrightarrow (4,2)$ interdot transition are shown in the Supplemental Material [31]. The data sets are consistent with Fig. 2: we observe a strong harmonic response near $\epsilon_0 = 0$ with harmonics out to $n = 4$ and no harmonic response is observed in the far-detuned regime. Additionally, measurements of ΔI_{res} as function of ϵ_0 for $f = 4.7$ GHz and $2eV_{ac} = 3.2$ meV show a sinusoidal-like modulation with ϵ_0 and a modulation frequency that increases with n (see the Supplemental Material [31]). The data contain the same odd or even structure shown in Fig. 2, where odd harmonics result in increased Pauli blockade leakage current, while even harmonics show a suppression of current. Another complete data set acquired at the $(7,1) \leftrightarrow (8,0)$ transition is consistent with these results, indicating that the observed effects are likely independent of the DQD charge occupancy.

In summary, we observe strong harmonic generation in electrically driven spin resonance. Up to eight harmonics are observed near the interdot charge transition. In contrast, at large detunings, only the fundamental EDSR response is observed. The strong detuning dependence illustrated by the data in Fig. 2 indicates that Landau-Zener transition physics may play an important role in the generation of the harmonic response observed near $\epsilon_0 = 0$.

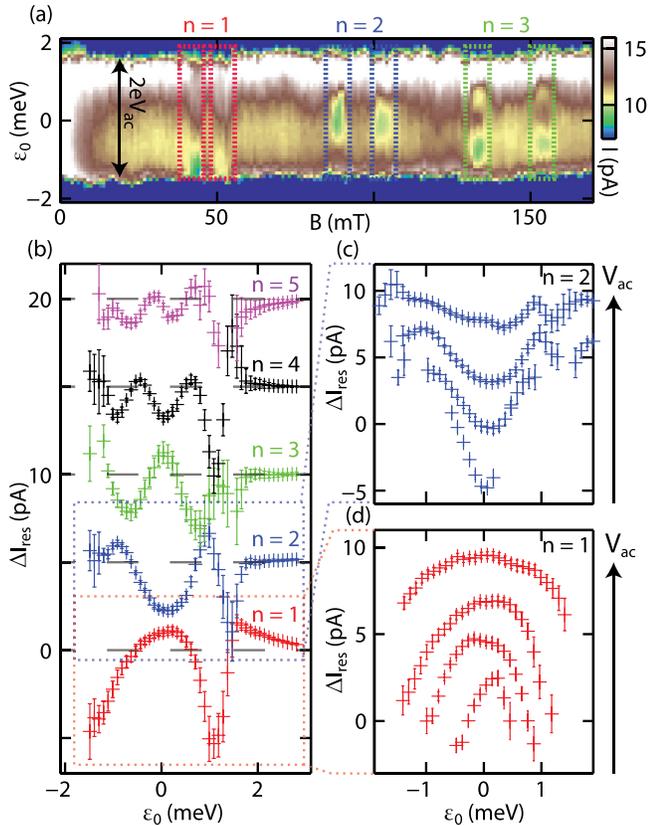


FIG. 3 (color online). (a) I as a function of B and ϵ_0 under continuous microwave driving with $f = 4.86$ GHz and $2eV_{ac} = 2.6$ meV. (b) Extracted resonant current ΔI_{res} for the $n = 1$ to $n = 5$ harmonics. The signal exhibits a sinusoidal-like modulation as a function of ϵ_0 . Successive traces are offset by 5 pA for clarity. ΔI_{res} for the $n = 1$ and $n = 2$ (c) harmonics for $2eV_{ac} = 1, 1.8, 2.6, 3.4$ meV, respectively. Successive traces are offset by 3 pA for clarity.

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